



Robert

## 06: Analysis of Graphs

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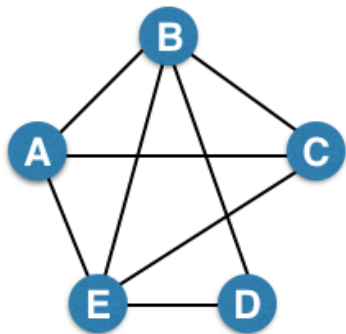
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Help

<b>Number of questions:</b>	4
<b>Positive points per question:</b>	3.0
<b>Negative points per question:</b>	1.0

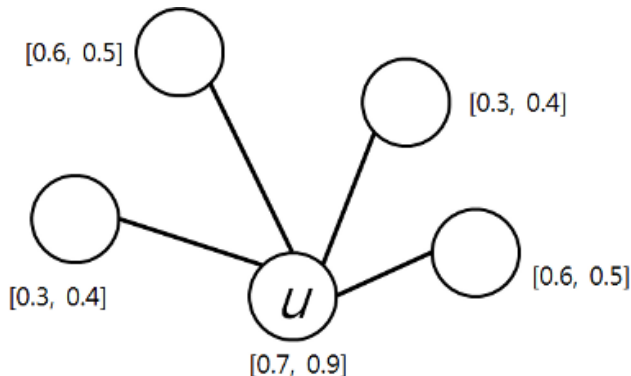
Gradiance quiz on Graph Analysis. You can attempt to answer the questions as many times as you like. Questions get randomly regenerated each time. The score of the \*last\* submission gets saved into our records (that is, once you get a perfect score, don't submit again with a bad one).

1. Consider the following undirected graph (i.e., edges may be considered bidirectional):



Run the "trawling" algorithm for finding dense communities on this graph and find all complete bipartite subgraphs of types  $K_{3,2}$  and  $K_{2,2}$ . Note: In the case of  $K_{2,2}$ , we consider  $\{\{W, X\}, \{Y, Z\}\}$  and  $\{\{Y, Z\}, \{W, X\}\}$  to be identical.

- ☐ a) There are 5 instances of  $K_{2,2}$ .
  - ☐ b) There are 6 instances of  $K_{2,2}$ .
  - ☐ c) There are at least 2 instances of  $K_{3,2}$ .
  - ☐ d)  $\{\{A, B\}, \{D, E\}\}$  is an instance of  $K_{2,2}$ .
2. You are running BigCLAM on a network of 1 billion nodes to detect two communities in the following way. At each iteration, you choose a node  $u$  and update community membership factor  $F_u$  of the node. Due to memory limit, you can query the information only for the neighbors of node  $u$  (not all the other nodes in the network). Imagine that you are looking at the following node  $u$  who has four neighbors:



Numbers in the bracket denote the value of community membership factors of each node. You are also given that the sum of  $F$  for all the nodes in the entire network (including the nodes not shown in the above figure) is  $[100.0, 1000.0]$ . Now, you want to compute likelihood  $l(u)$  at the current values of  $F$ :

$$l(u) = \sum_{v \in N(u)} \log(p(u, v)) + \sum_{v \notin N(u)} \log(1 - p(u, v))$$

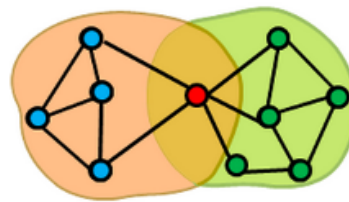
where  $p(u, v)$  is the BigCLAM edge probability and  $N(u)$  is the set of neighbors of node  $u$ . Since the first term can be trivially computed from the information shown in the figure, we are interested in computing the second term, namely  $l'(u)$ :

$$l'(u) = \sum_{v \notin N(u)} \log(1 - p(u, v))$$

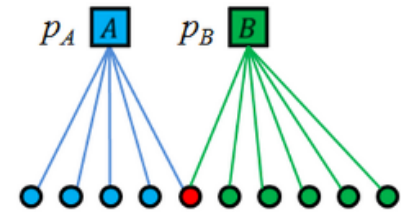
Compute the value of  $l'(u)$ .

- ☐ a) -965.82      ☐ b) -97.56      ☐ c) -43.54      ☐ d) -857.54

3. We fit AGM to the network on the left, and found the parameters on the right:



Network



Learned AGM parameters

Find the optimal values for  $p_A$  and  $p_B$ .

- ☐ a)  $p_A = 0.8$   
☐ b)  $p_A = 0.7$   
☐ c)  $p_B = 0.5$   
☐ d)  $p_B = 0.3$

4. A bipartite graph has nodes  $a_i$  and  $b_i$  for  $i = 0, 1, \dots, 5$ . There is an edge between  $a_i$  and  $b_j$  if  $i-j$  is divisible by 2 or 3. For example,  $a_0$  is connected to  $b_0, b_2, b_3$ , and  $b_4$ . Also,  $a_3$  is connected to  $b_0, b_1, b_3$ , and  $b_5$ . Another way to understand this graph is to realize that  $a_i$  is connected to  $b_j$  unless  $j = i+i$  or  $j = i-1$ , where arithmetic is modulo 6.

Say a complete bipartite subgraph is *maximal* if no nodes can be added to it and the "complete" property be maintained. Which of the following instances of  $K_{2,2}$  is NOT maximal?

- ☐ a)  $\{a_2, a_5, b_2, b_5\}$   
☐ b)  $\{a_0, a_3, b_0, b_3\}$   
☐ c)  $\{a_1, a_3, b_3, b_5\}$   
☐ d)  $\{a_2, a_3, b_0, b_5\}$