

# Analyzing Political Relationship Structure in the U.S. Congress

Lucas Lin  
Stanford University

lucaslin@stanford.edu

Andrew Zhang  
Stanford University

azhang97@stanford.edu

## Abstract

*We analyzed the evolving structure in political networks by examining the voting patterns across sessions for the U.S. Congress. This analysis includes graph similarity across the time domain, measures of clustering, polarization, and identification of positive and/or antagonistic links across clusters. We show that various techniques of modularity, cohesion, and graph similarity can be applied to analyze the political structure of the U.S. Congress. Using it, we see key historical events and climate supported by the data analyses. Most evidently, we see that the U.S. Congress is seemingly increasingly polarized compared to previous Congress sessions.*

## 1. Introduction

In this paper, we will be examining the voting patterns across sessions for the U.S. Congress. This analysis includes graph similarity across the time domain, measures of clustering and cohesion, and examining modularity as a measure of polarization. Such analysis could uncover interesting trends including the progression of increasing polarization in recent years and looking for emergent community structures.

More useful to citizens, however, is the fact that such analysis allows citizens to evaluate the performance of their elected officials. In modern society, complex voting campaigns

and obfuscation of congressional activities can obscure the true leanings and activities of congressmen/women. This kind of analysis can be used to quantify the degree of political affiliation of each Congress member

Previous research shows that there is a space for further research on political networks, and perhaps the U.S. Congress in particular. Using graph formulation methods, methods of determining polarization, graph similarity, and more, there are a solid set of manipulation and metrics algorithms to produce interesting information about political networks. We look to specifically examine the U.S. Congress political alliance network, see it as it evolves over time, make comparisons between the Senate and the House, and also make comparisons with other countries' social political structure.

## 2. Previous Research

### 2.1. Voting Behavior, Coalitions and Government Strength through a Complex Network Analysis (Maso et al. 2014) [2]

This paper utilizes tools from Complex Network literature to introduce metrics for measuring the extent of party polarization, the internal cohesiveness of each party, and stability of the current majority government coalition.

The concepts of centrality and density are im-

portant tools for examining emergent community structures in graphs. In the case of politics, access to the voting patterns of representatives enables us to analyze their political stances without the need for more discrete knowledge. Therefore, it's important to develop appropriate metrics to measure success of our graph algorithms.

The other papers we have examined propose methods of developing a graph from the data and analyzing their similarity across time steps. This paper serves to provide the metrics by which we can evaluate each time step, which will help us demonstrate quantitative change in the political landscape over time.

The use of Italian Chamber data certainly provides compelling results to back up the methods suggested by the paper. Its metrics for cohesiveness accurately predict which coalitions are in support and in opposition of the majority coalition. Furthermore, two coalitions of the Italian Chamber showed a reduction in internal cohesiveness and promptly broke down over a 6 month time period. Their results also clearly demonstrate a subsequent notable decrease in the cohesion of majority and opposition sides, along with an increase in polarity.

## **2.2. The backbone of bipartite projections: Inferring relationships from co-authorship, co-sponsorship, co-attendance and other co-behaviors (Neal 2014) [3]**

This paper proposes a new method that extracts the backbone from bipartite projections using the stochastic degree sequence model (SDSM), which involves the construction of empirical edge weight distributions from random bipartite networks with stochastic marginals. Furthermore, it demonstrated this algorithm using data on bill sponsorship in the 108th U.S. Senate, which seemed to be a good starting point to determine behavior and characteristics of the U.S. Congress.

Bipartite projections are an important methodological tool for analyzing natively one-mode networks that are unable to be observed practically. In the case of political environments, collection of data on political alliances and collaboration is frequently unobtainable due to strategic reasons on the politicians' part, so bipartite projections on co-sponsorship, co-voting, and other joint activities can be used to infer information about the network of interest. As a result, the proxy measurement tool that is the bipartite graph requires a construction method that handles additional consideration of edge weights in order to make inferences meaningful.

In the example of the co-sponsorship in the U.S. Senate, the paper mentions the fact that different senators have differing propensities to collaborate—some co-sponsoring far more than others—and some bills or motions are far less controversial than others—some procedural motions being completely unanimous. It becomes necessary to take into account these factors when generating the bipartite graph to analyze lest the inferences made become faulty. The SDSM method mentioned earlier views the observed bipartite network of co-sponsorship as one of the many possible outcomes of an unobserved, stochastic process of agent-to-artifact matching driven by probabilities derived from the likelihood a given agent (senator) will be linked to a given artifact (bill/motion). SDSM estimates these probabilities and generate random bipartite networks and then uses the meaningful differences in the observed network with the generated network in order to parse out stronger-than-average political alliance links or negative antagonistic links between agents.

### 2.3. Algorithms for Graph Similarity and Subgraph Matching (Koutra et al. 2011) [1]

In this paper, Koutra et al. develops algorithms for the related problems of graph similarity and subgraph matching, which are problems useful in several different fields of graph analysis. Specifically, we investigated the new framework the paper created for determining graph similarity using belief propagation and related ideas.

Formally, they assert the problem of graph similarity to be: Given two graphs  $G_1(n_1, e_1)$  and  $G_2(n_2, e_2)$ , with possibly different numbers of nodes, edges, and mapping, find a measure of similarity that captures the intuition of the two graphs' similarity. Using the key idea that "a node in one graph is similar to a node in another graph if their neighborhoods are similar", the paper creates a method to capture both the local and global topology of the graphs and deal with connected and disconnected graphs.

Loopy belief propagation is an algorithm that uses a propagation matrix and prior state assignment to infer the maximum likelihood state probabilities of all the nodes in the Markov Random Field. In this framework, nodes pass information to neighbors iteratively until convergence. Koutra et al. leverages belief propagation for graph similarity by initializing all nodes to a prior belief  $p$ , running belief propagation for both graphs and getting a similarity measure by taking the vectors of the final beliefs from the two graphs. The paper mentions both a naive  $O(n^2)$  implementation of the belief propagation method as well as a scalable and fast approximation of belief propagation in order to create a linearized graph similarity algorithm.

## 3. Data Collection

We use the voting data provided by the Senate [5] and House [4], which are then compiled and

made available by ProPublica Data Store in their ProPublica Congress API. This endpoint includes voting information for the House and Senate, including the outcome of each vote, number of votes for each side, cosponsorship by Congress members, and each Congress member's stance on each topic. Most of the data in the ProPublica Congress API is updated daily, while votes are updated every 30 minutes.

In order to collect the data and formulate it into graphs, we make use of ProPublica's RESTful API and first retrieve a list of all members in a certain Congress session. Then, we iterate through all combinations of these members to find cosponsorship data and voting data. At the same time, we receive the bill number for each cosponsored bill and also make a separate request to the endpoint in order to store the data locally. From the member, bill, cosponsorship, and voting data, we initially generate two graphs: a bipartite graph consisting of members and bills based off cosponsorship and a bipartite graph consisting of members and bills based off of voting. Then, we fold both graphs based on the bills that members are either cosponsored to or covoting for.

## 4. Methods and Evaluation

Our first step involves constructing two graphs, where each node represents a member of Congress, and edges connecting nodes are weighted by metrics that measure the strength of political similarity between the congressmen.

Therefore, there must exist an edge between any two nodes. It follows that for both graphs, we ideally need metrics that result in weighted graphs where the weights are  $0 \leq w_{ij} \leq 1$ .

#### 4.1. Cosponsorship

Our cosponsorship graph  $G_C$  is a weighted, directed graph. Each edge weight is determined by

$$w_{ij} = \frac{\# \text{ bills cosponsored between } i \text{ and } j}{\# \text{ bills sponsored by } i}$$

#### 4.2. Voting Patterns

Our voting pattern graph  $G_V$  is a weighted, undirected graph. For each session of Congress, we build a separate graph by counting the number of times each pair of Congress members vote in the same way (i.e. both in favor, against, or abstain from voting). Then, we normalize each edge by the total number of votes in the session.

This limits the weights to the range  $[0,1]$ , where a weight of 1 is achieved by two Congress members if they voted the exact same in every vote of the session.

#### 4.3. Metrics for Cohesion of Political Party

Let us first consider a weighted graph  $G$  with  $n$  nodes, and each political party as a group  $P$  with  $n_P$  Congress members. We can define weighted link density of the subgraph as

$$d_{int}(P) = \frac{\sum_{i,j \in P} w_{ij}}{n_P(n_P - 1)/2}$$

We call this  $d_{int}$  as it refers to the intra-cluster density of possible weights. Similarly, we can define

$$d_{ext}(P) = \frac{\sum_{i \in P, j \notin P} w_{ij}}{n_P(n - n_P)}$$

which refers to the inter-cluster density of possible weights.

These can be compared to the total clustering density of the graph  $G$  with  $n$  nodes,

$$d(G) = \frac{\sum_{i,j \in G} w_{ij}}{n(n - 1)/2}$$

If the intra-cluster density of a particular party subgraph  $d_{int}(P)$  is high compared to the benchmark  $d(G)$ , this reflects strongly upon the party's cohesion: they vote similarly. Likewise, a low  $d_{ext}(P)$  suggests that the party votes less frequently with the opposing party.

#### 4.4. Modularity and Polarization

For undirected graphs, we have modularity

$$Q = \frac{1}{2W} \sum_{i,j} \left( A_{ij} - \frac{d_i d_j}{2W} \right) \delta(C_i, C_j)$$

where  $W$  is the total weight in the network,  $d_i$  is the degree of each node, and  $\delta(C_i, C_j)$  is 1 if the  $i$  and  $j$  are in the same community, and  $A_{ij} = w_{ij}$  is the weight of the edge between nodes  $i$  and  $j$ .

However, for a directed graph, we can add a slight modification to the formula.

$$Q = \frac{1}{W} \sum_{i,j} \left( A_{ij} - \frac{d_{i,out} d_{j,in}}{W} \right) \delta(C_i, C_j)$$

where  $d_{i,out}$  is the outdegree of node  $i$  and  $d_{j,in}$  is the indegree of node  $j$ , and  $A_{ij} = w_{ij}$  is the weight of the directed edge out of node  $i$  and in to node  $j$ .

Ideally, the modularity is maximized by grouping members by their party alignments. To this end, we can measure the polarity of the political divide by calculating the differences in modularity,  $dQ$ , associated with moving one member to his/her opposing party. Large values of  $dQ$  indicate that members work as a cohesive whole. However, if both sides have a majority of large  $dQ$ s, we can demonstrate a polarizing effect between the political parties.

#### 4.5. Graph Similarity

The problem of graph similarity in the context of longitudinally comparing different Congress sessions requires finding some metric of similarity with unknown node correspondences, since

congressmen change over time. We use a variation on the  $\lambda$ -distance spectral method to derive similarity between graphs—which are directed and weighted. We extract the eigenvalues of the normalized Laplacian of each graph and then find the Euclidean distance between these eigenvalues to serve as our similarity metric.

## 5. Results

Figures 1,2,3 show the change in party cohesion with either the Senate or the House over time using different metrics. For all these graphs, the blue left side represents the congressmen affiliated with the Democratic Party and the red right side represents the congressmen affiliated with the Republican Party. The dark colored lines on these graphs is the link density of members of the same party which represents the likelihood of congressmen working together within their own party. The light colored lines on these graphs is the link density of members with the opposing party which represents the likelihood of congressmen working together with members of the opposing party. The black dotted line represents the link density of the entire Congress chamber and serves as a benchmark. We note that  $d_{int}$  of each party is always at least greater than or equal to  $d(G)$  and that  $d_{ext}$  of each party is always at least less than or equal to  $d(G)$ . From a political standpoint, this makes a lot of sense considering that members of the same party tend to agree more with each other, collaborate more together, and vote in more similar manners.

Examining Figure 1, we see a couple of general trends in party cohesion in Democrats and Republicans from the 93rd Congress to the 114th Congress. First, on balance, it seems that the difference between  $d_{int}$  and  $d_{ext}$  is smaller in older sessions and gradually gets larger as we come to the more recent sessions. Notably in the 95th Congress, we see the polarity between both parties at a minimum. This can be attributed to that fact that during this session, Both chambers

had a Democratic majority and it was the first time either party held a filibuster-proof 60% super majority in both the Senate and House chambers since the 89th United States Congress in 1965. In this heavily Democratic leaning climate before the surge of divisive politicking seen today, it makes sense that especially in the realm of bill cosponsorship—which is seen as a show of support—that both parties put aside differences to create legislation together without much issue. This was further supported by the fact that the current president at the time, Jimmy Carter, was widely considered to be undistinguished and that he lacked an overriding design for what he wanted his government to do. Uncontroversial attitudes and plans defined this session. However, in the 104th Congress, which is the first time the Republicans had a majority in both houses since 1950s, there is a sharp decrease in cosponsorship and covoting among Republicans towards the Democrats. This coincides with the the “Republican Revolution,” as the aftermath of the 1994 elections, which empowered Congressional Republicans led by Speaker of the House Newt Gingrich to propose several conservative policies. Disagreements with Congressional Republicans led to two shutdowns of the federal government between 1995 and 1996, which is shown by the unwillingness of the Republicans to work with the Democrats at this time.

We see that Figure 2 echoes much of the same trends that we saw in Figure 1. What is of note is that the cosponsorship levels in the House of Representatives are initially very low compared to the Senate (until the 96th Congress). We know that only since 1967 did congressmen in the House of Representatives have the ability to express support for a piece of legislation by signing it as a cosponsor whereas congressmen in the Senate had this ability since the mid-1930’s. It then makes sense that we see an initial lower usage of cosponsorship in the 1970s for the House of Representatives as they become accustomed to

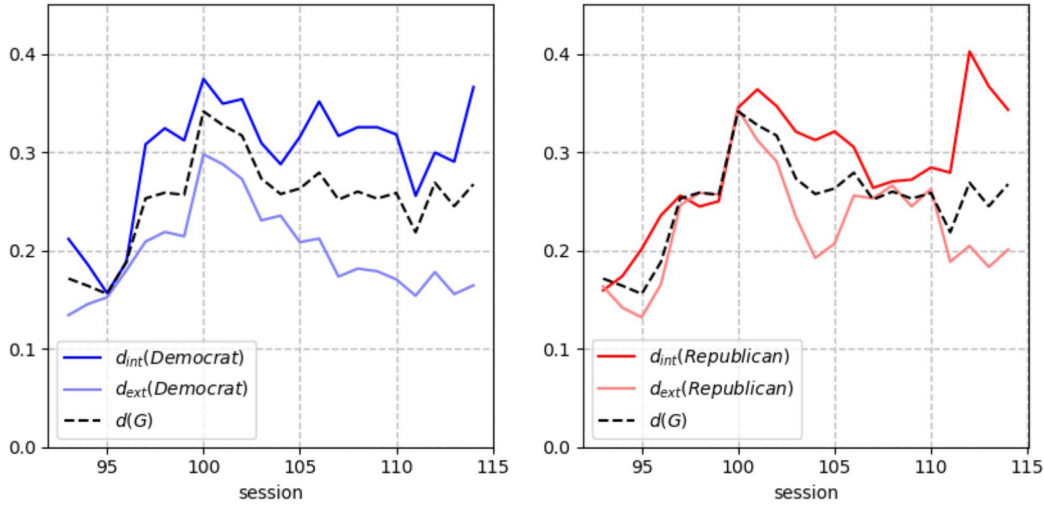


Figure 1. Measure of Party Cohesion in the Senate using Bill Co-Sponsorship

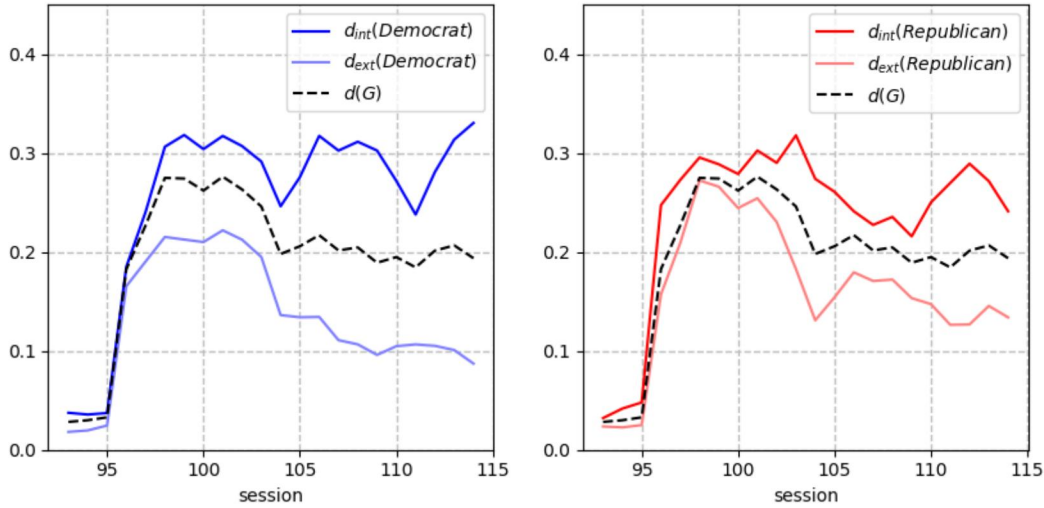


Figure 2. Measure of Party Cohesion in the House of Representatives using Bill Co-Sponsorship

using it as a tool in the political arena. Another session to note is the 112th Congress. This time coincides with the 2010 midterm elections where the Republican Party won the majority in the House of Representatives while the Democrats kept their Senate majority. This was the first Congress in which the House and Senate were controlled by different parties since the 107th Congress. We see a slight increase in the  $d_{int}$  of both parties in the House but not their  $d_{ext}$  whereas in the Senate, both parties had both  $d_{int}$  and  $d_{ext}$  slightly increase. What is interesting to

note is that in such a relatively even climate, we see the propensity for the Senate to be the slightly less divisive chamber due to the likelihood of working or voting together with the opposing party to be greater than that of the House. This aligns with the idea that the Senate was intended to be the more deliberative body, impacted less by the winds of politics and more given to in-depth examination.

Looking at Figures 1 and 3 The biggest difference between the party cohesion study through

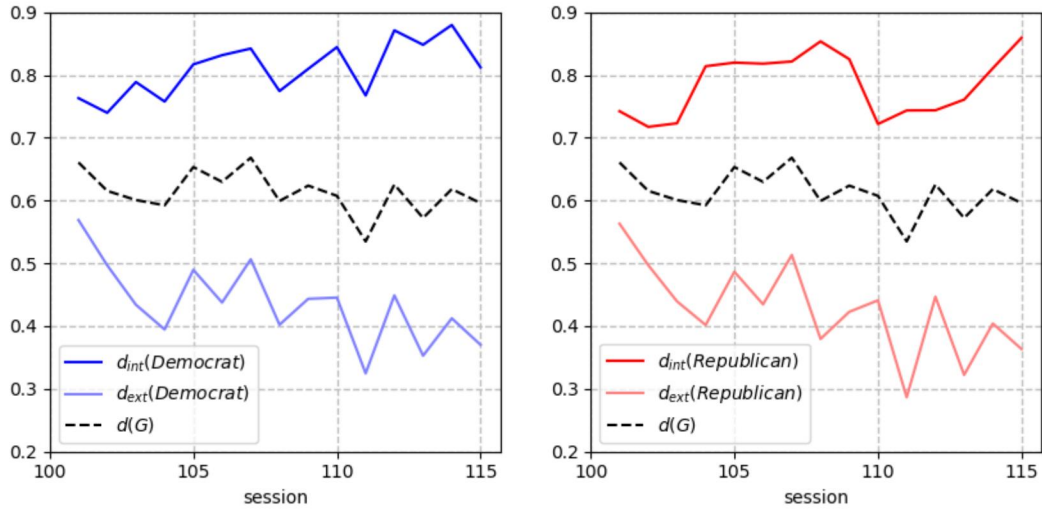


Figure 3. Measure of Party Cohesion in the Senate using Co-Voting

cosponsorship versus covoting is that the party polarization is a lot more evident. This makes sense because it is easy for a congressman to simply attach their name to a bill that probably is bipartisan in nature in order to show that they are cooperating with the other party. However, in the realm of voting, since every congressman has to make a decision on which way to vote on every single bill, allegiances can be more clearly delineated using covoting as part of the metric. One thing of note in Figure 3 is the sharp drop in external party covoting at the 111th Congress. The 111th Congress mostly spanned the first two years of Barack Obama's presidency. In the November 4, 2008 elections, the Democratic Party increased its majorities in both chambers, giving President Obama a Democratic majority in the legislature for the first two years of his presidency. During this time, the Democratic Party essentially unilaterally passed many more liberal pieces of legislation that were all opposed by the current Republicans at the time, resulting in the separation between Democrat and Republican covoting.

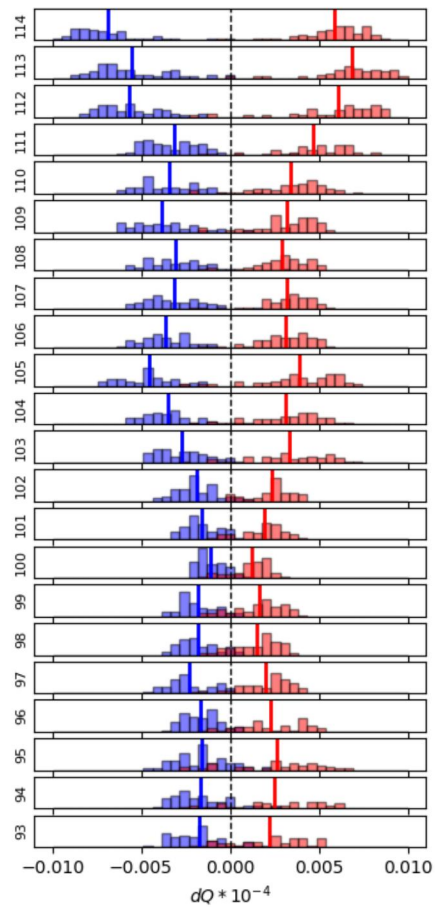


Figure 4. Modularity Deltas in the Senate using Co-Sponsorship

The series of histograms in Figure 4 show the modularity deltas of Senate congressmen using cosponsorship as the primary metric. The histograms show the changes in modularity if a congressman were to switch to the opposing party. The black dotted line in the center represents no modularity change and the solid colored lines represent the median of each party. What we see with this series of modularity delta histograms is that the later Congress sessions see a much larger magnitude in modularity change than earlier Congresses. This means that congressmen have become increasingly polarized and party oriented since the 93rd Congress, tending to cosponsor bills more and more with only their own party members.

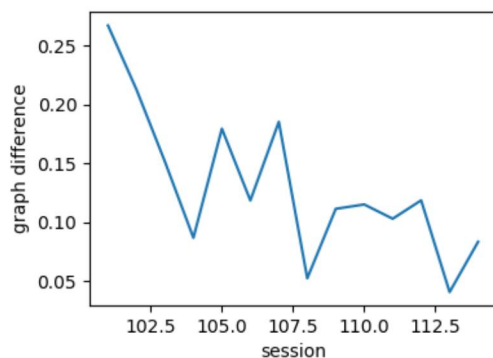


Figure 5. Similarity of Historical Congresses to the 115th Congress

In Figure 5, we see a trend of decreasing graph distance compared to the 115th Congress from older sessions to newer sessions. This represents the fact that the way congressmen do their work in the political arena do change over time and helps show the fact that party polarization is occurring as well.

## 6. Difficulties

We have encountered many difficulties when trying to move forward with this project. First, open data of Congress sessions is a relatively new idea that has been embraced, so official channels of data distribution is rather new. As a result,

there are occasionally observed missing spots in data. Furthermore, working with the ProPublica API meant that we had to wait through a the process of obtaining an access key as well as working within the request rate limits which made data collection exceptionally slow. Coupled with the fact that the API was not documented correctly in some places and had random errors for certain combinations of congressmen when looking at cosponsorship and voting similarity data, meant that a lot of time was spend on data collection and cleaning.

## 7. Conclusion

We have shown that various techniques of modularity, cohesion, and graph similarity can be applied to analyze the political structure of the U.S. Congress. Using it, we see key historical events and climate supported by the data analyses. Most evidently, we see that the U.S. Congress is seemingly increasingly polarized compared to previous Congress sessions.

### 7.1. Future Work

Using similar techniques it would be interesting to see how the U.S. Congress’s political relationship structure compares to other countries. Similarly if we could obtain reliable data from even earlier Congresses we could then see how much difference centuries have on poltlical structure.

## References

- [1] D. Koutra, A. Parikh, A. Ramdas, and J. Xiang. Algorithms for graph similarity and subgraph matching. 2011. Presented at the Ecological Inference Conference.
- [2] C. Maso, G. Pompa, M. Puliga, G. Riotta, and A. Chessa. Voting behavior, coalitions and government strength through a complex network analysis. *PLoS One*, 9, 2014.
- [3] Z. Neal. The backbone of bipartite projections: Inferring relationships from co-authorship,



co-sponsorship, co-attendance and other co-behaviors. *Social Networks*, 39, 2014.

[4] U. H. of Representatives. Roll call votes.

[5] U. S. Senate. Roll call votes.