

# Reasoning in Knowledge Graphs Using Embeddings

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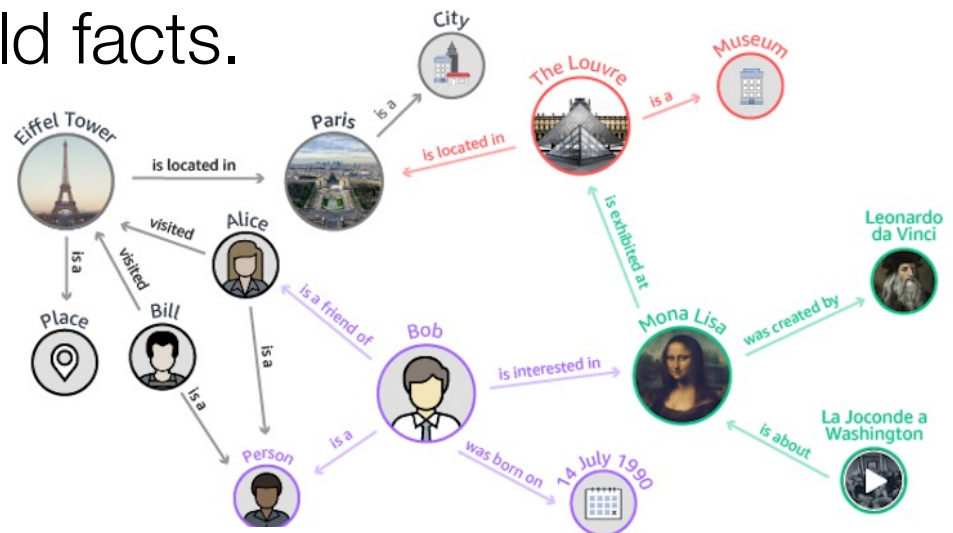
Joint work with W. Hu, H. Dai, B. Dai, X. Chen, M. Yasunaga, H. Sun, D. Schuurmans, D. Zhou, A. Mousavi, T. Rekatsinas, I. Ilyas, J. Leskovec



# Knowledge Graphs

- Knowledge Graphs are **heterogenous** graphs
  - $\mathcal{G} = (\mathcal{V}, \mathcal{E}, \mathcal{R})$
  - $\mathcal{V}$ : node set;  $\mathcal{E}$ : edge set;  $\mathcal{R}$ : relation set;
  - Each edge  $e \in \mathcal{E}$  represents a fact  $(v_s, r, v_o)$  over subject  $v_s$  and object  $v_o \in \mathcal{V}$  with relation  $r \in \mathcal{R}$ .
  - KGs capture real world facts.

- Examples:

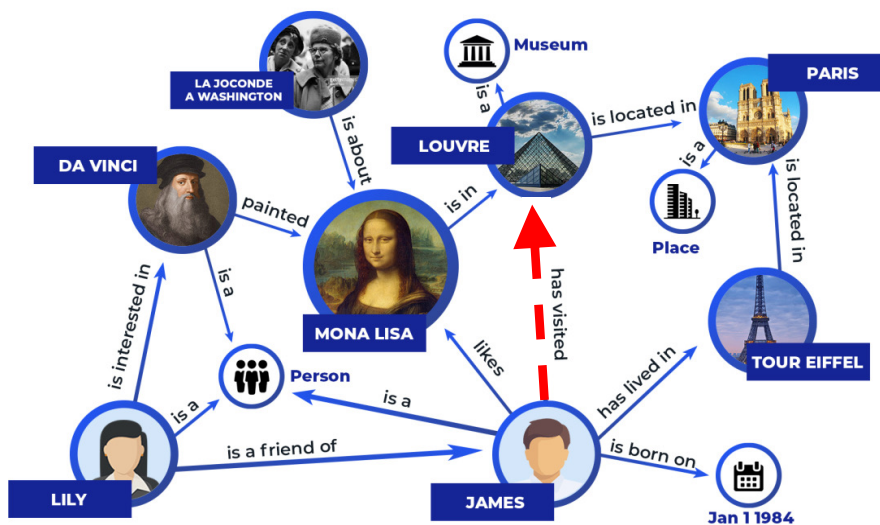


# Traditional Tasks

## Knowledge Graph Completion

Given the existing edge set  $\mathcal{E}$ , predict the missing object for a given triplet  $(v_s, r, v_t)$

Example: Is **Louvre** an object to (**James**, **Visited**, ?)



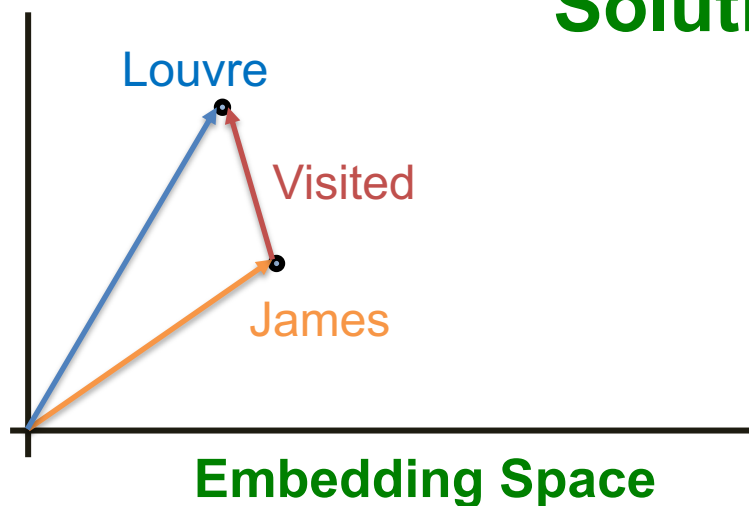
# Traditional Tasks

## Knowledge Graph Completion

Given the existing edge set  $\mathcal{E}$ , predict the missing object for a given triplet  $(v_s, r, v_t)$

Example: Is Louvre an object to (James, Visited, ?)

### Solution: TransE



TransE learns an entity embedding matrix and a relation embedding matrix, such that given a triplet  $e = (v_s, r, v_t) \in \mathcal{E}$ , we have  $\mathbf{v}_s + \mathbf{r} = \mathbf{v}_t$ , where  $\mathbf{v}_s, \mathbf{r}, \mathbf{v}_t \in \mathbb{R}^d$ .

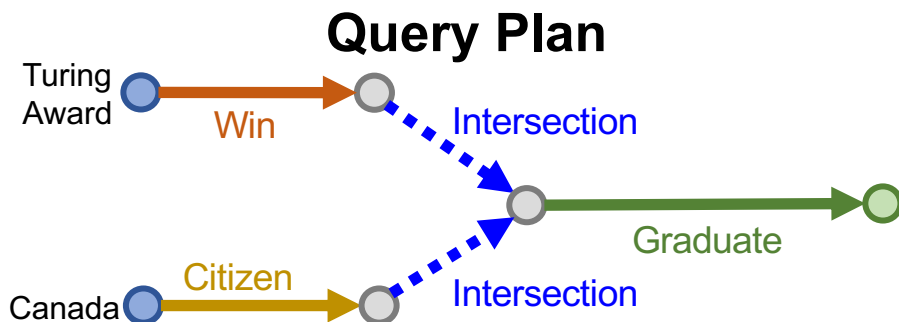
# Our Task: Multi-hop Reasoning

## Answering Acyclic Conjunctive Queries

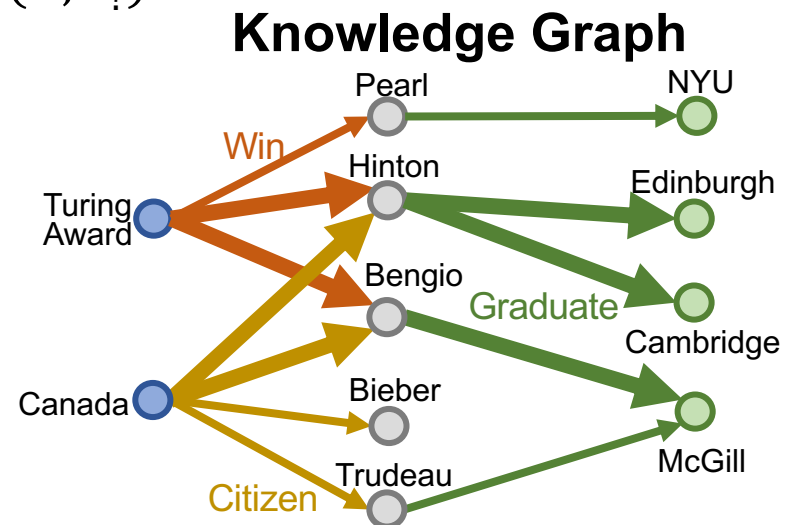
- A subset of **first-order logic** with existential quantifier ( $\exists$ ), conjunction ( $\wedge$ )

“Where did all Canadian citizens with Turing Award graduate?”

**Input:**  $q = V_? . \exists V : \text{Win}(\text{TuringAward}, V) \wedge \text{Citizen}(\text{Canada}, V) \wedge \text{Graduate}(V, V_?)$



**Output:** {Edinburgh, Cambridge, McGill}

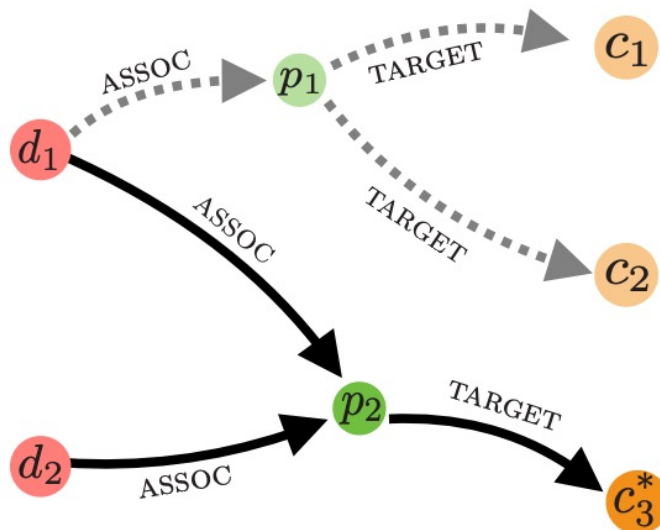
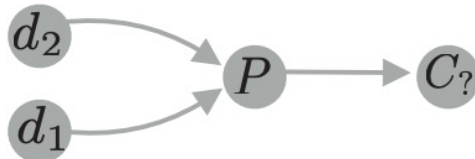


# Examples

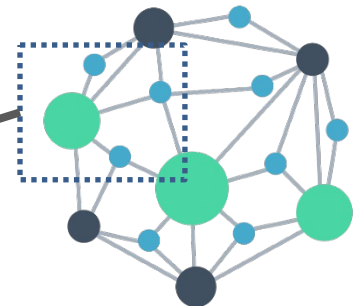
## Applications in biomedicine:

$C_?.\exists P : \text{ASSOC}(d_1, P) \wedge \text{ASSOC}(d_2, P) \wedge \text{TARGET}(P, C_?)$

“Predict drugs  $C_?$  that might target proteins that are associated with the given disease nodes  $d_1$  and  $d_2$ ”



Bio KG



# Why is it hard?

## Key challenges:

Big graphs and queries can involve **noisy** and **unobserved** data!



**93.8%** of people from Freebase have no place of birth and **78.5%** have no nationality!

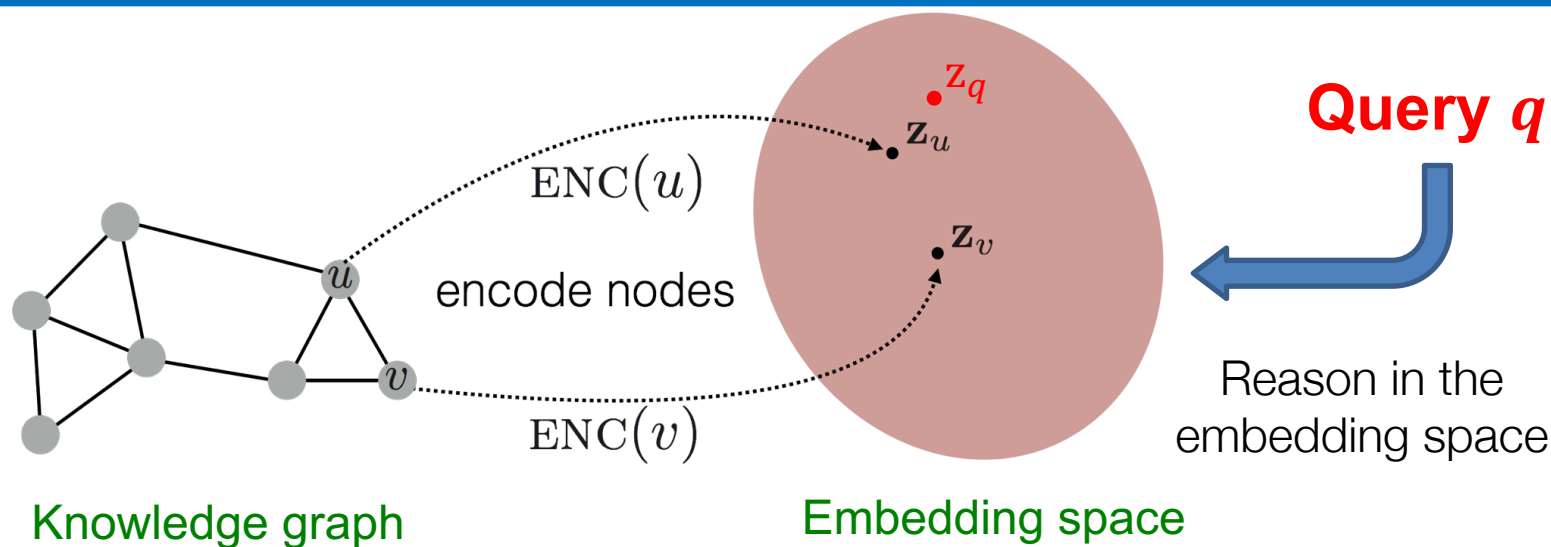


**98.12%** of movies recorded in 2020 have no information about their cost!

[\[Distant Supervision for Relation Extraction with an Incomplete Knowledge Base. Min et al., NAACL 2013\]](#)

[\[Enriching Wikidata with Linked Open Data. Zhang et al., 2022\]](#)

# Our General Idea



- **Reason in the embedding space:** Map the query and entities into **embedding space** such that answer entity embeddings are close to the query embedding (**contrastive learning**).
  - Low-dimensional embedding allows generalization.

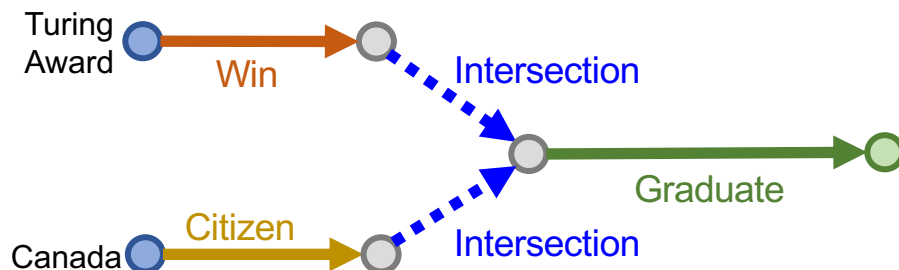
# How to Embed the Query?

- Embed the query following the query plan!

“Where did all Canadian citizens with Turing Award graduate?”

**Input:**  $q = V_? . \exists V : \text{Win}(\text{TuringAward}, V) \wedge \text{Citizen}(\text{Canada}, V) \wedge \text{Graduate}(V, V_?)$

## Query Plan

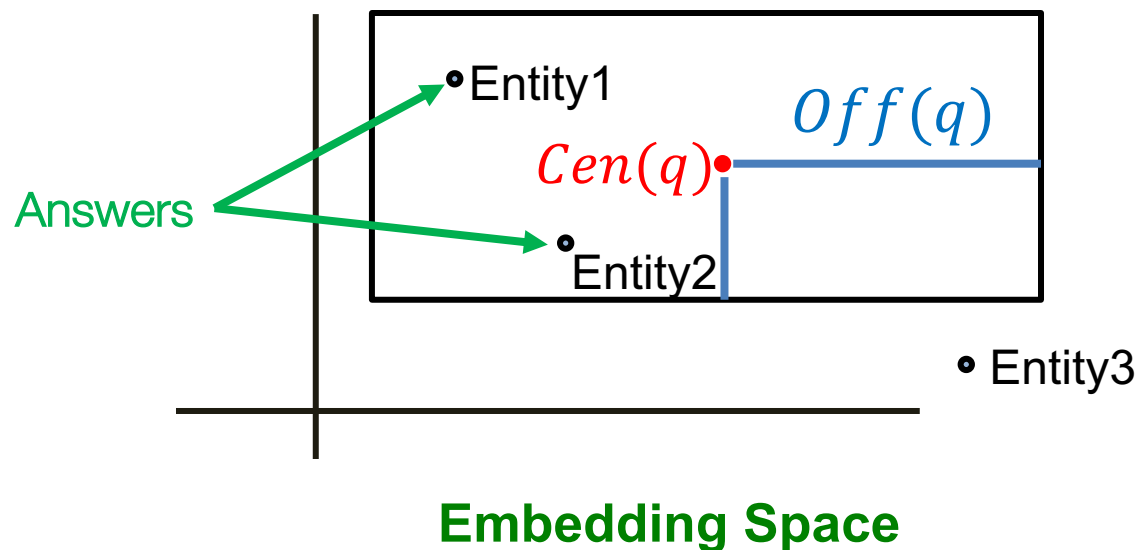


- Traversing query plan from leaves (anchors) until the root (answers)

# Our Model: Query2box

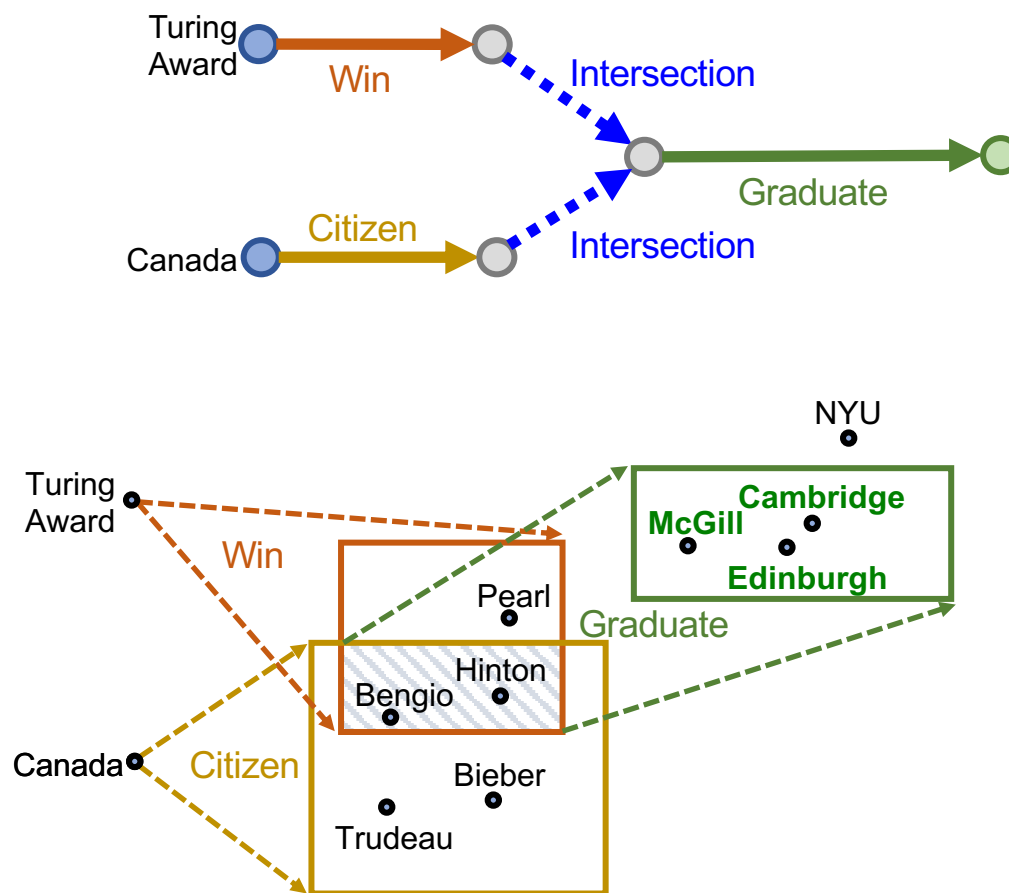
## Query2Box embedding:

Embed queries with hyper-rectangles (boxes):  $\mathbf{q} = (\text{Cen}(q), \text{Off}(q))$ .



# Example: Query2Box

“Where did Canadian citizens with Turing Award graduate?”



# Benefits of Query2Box

## **Scalability and efficiency:**

- Any query can be reduced to a couple of matrix operations and a single k-nearest neighbor search

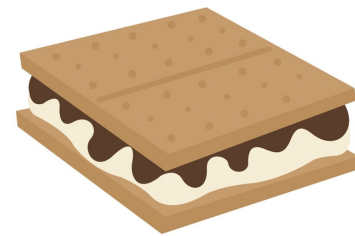
## **Generality:**

- We can answer any query (even those we have never seen before)

## **Robustness to noise:**

- Graph can contain missing and noisy relationships

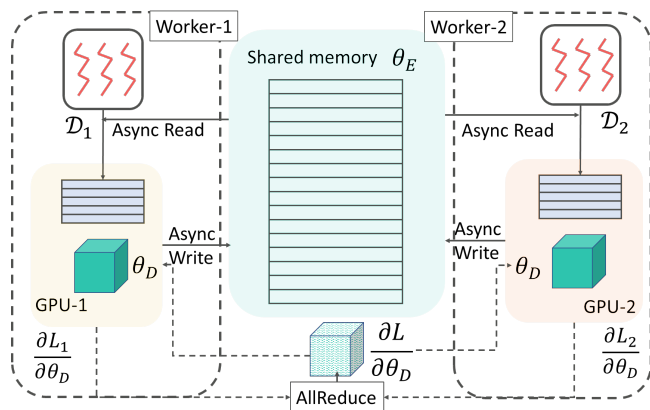
# Reasoning Framework: SMORE



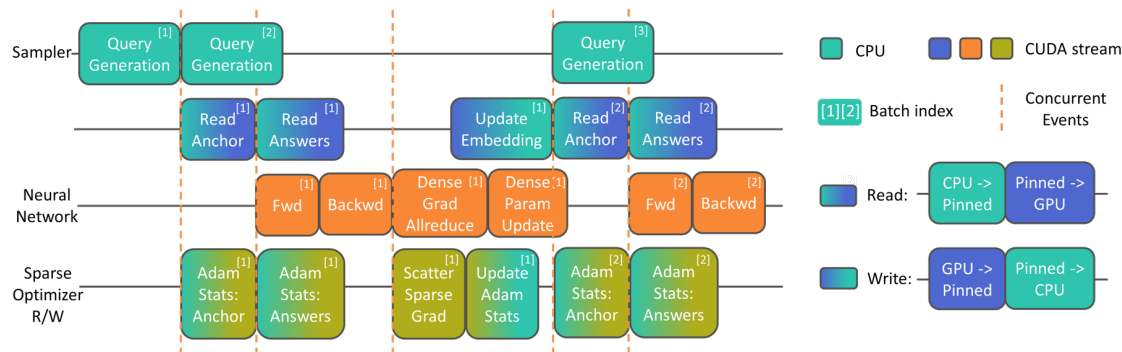
## Scalable Multi-hOp REasoning framework

First framework that scales reasoning algorithms to extremely large KGs (86m nodes, 338m edges)

### Distributed Paradigm

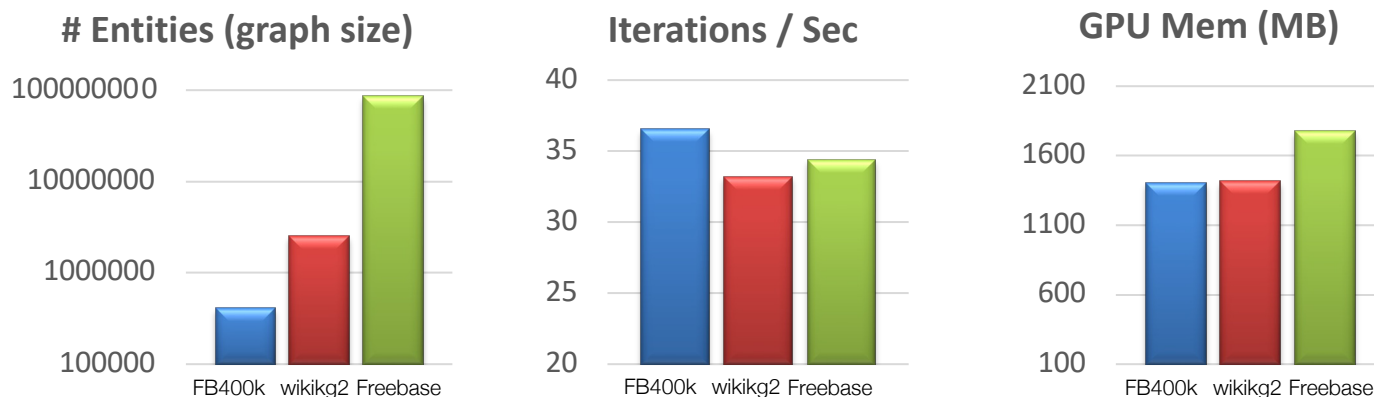


### Pipelined Asynchronous Design

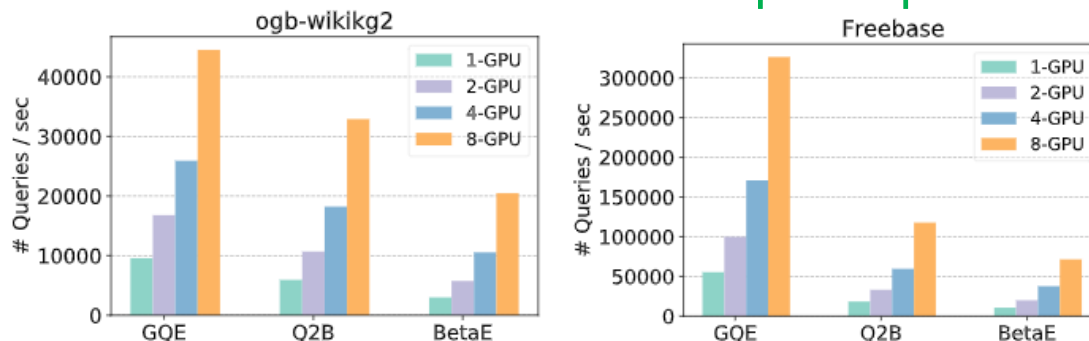


# SMORE on Massive KGs

- SMORE supports 6 different link prediction + multi-hop reasoning methods
- Prior implementation runs out of GPU memory and time limit on large KGs
- SMORE enables (almost) graph-size agnostic speed and GPU memory usage



- SMORE enables almost linear multi-GPU speedup



PR welcome!

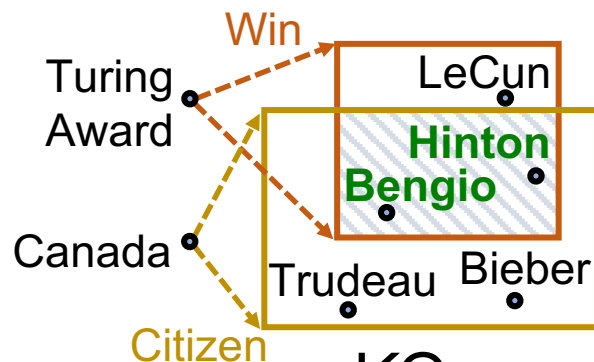
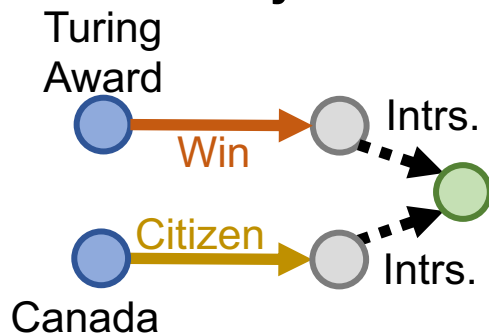


# Application (1): KG Question Answering

KGQA: Answering natural language questions over massive KGs

Question → Query Plan → Box Embedding

Who are Canadian Turing Award winners?

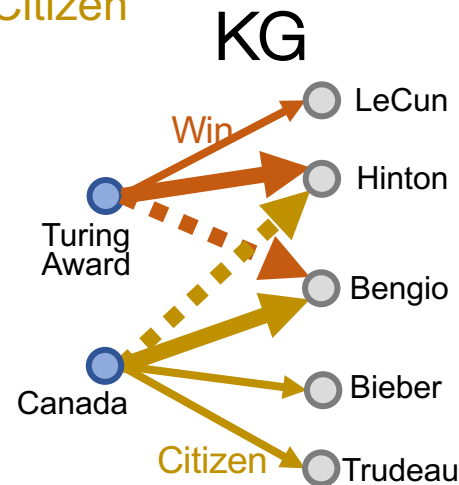


Our method: Latent Execution-Guided Reasoning

Given a question, we iteratively do

(start from an empty tree with mentioned entities as root)

- **Execution-guided synthesis**: synthesize one step (grow the query plan) based on the current query embedding.
- **Latent query execution**: execute the new step in the embedding space



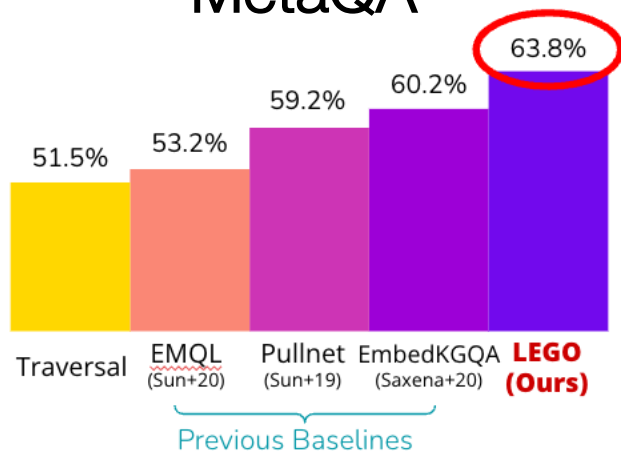
# Application (1): KG Question Answering

Our method: Latent Execution-Guided Reasoning (LEGO)

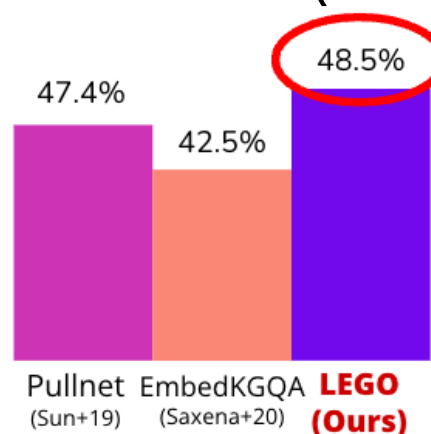
Questions	MetaQA	WebQuestion
Train	96,106	2,848
Dev	9,992	250
Test	9,947	1,639

KG	Entities	Relations	Observed Edges	Missing Edges
MetaQA	43k	18	134k	133k
WQSP	409k	1,836	2m	2m

## MetaQA



## WebQuestion (WQSP)



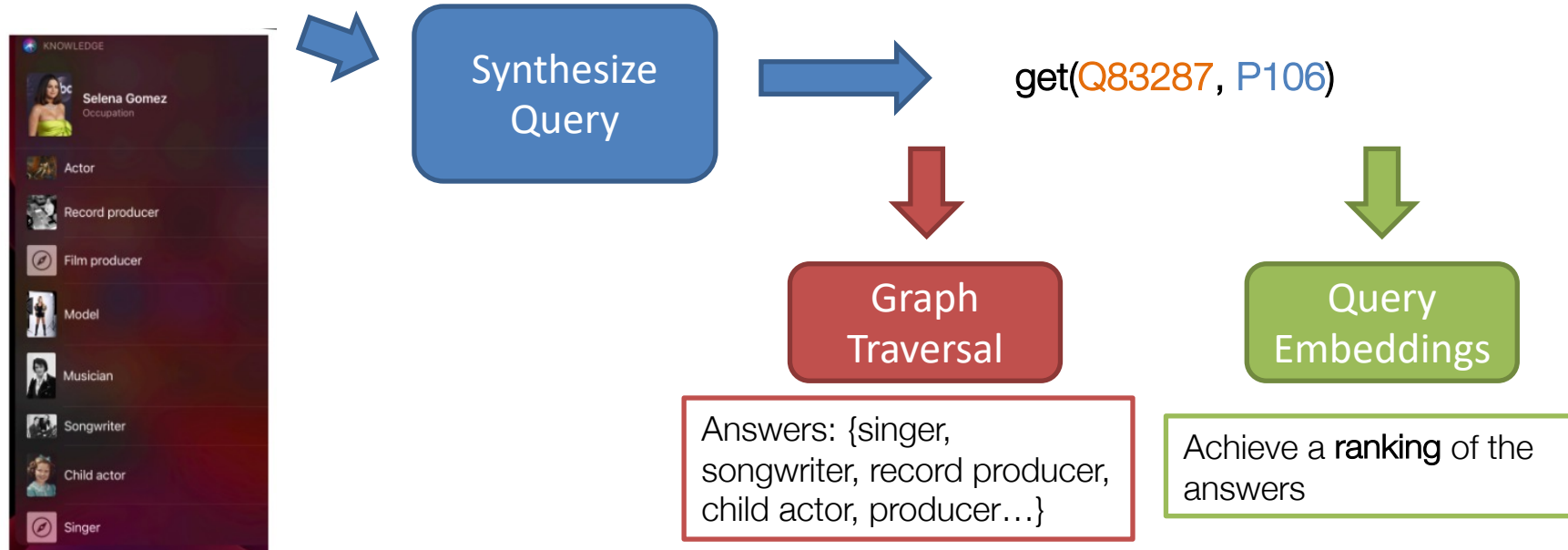
[\[Latent Execution-Guided Reasoning for Multi-Hop Question Answering. Ren et al., ICML 2021\]](#)



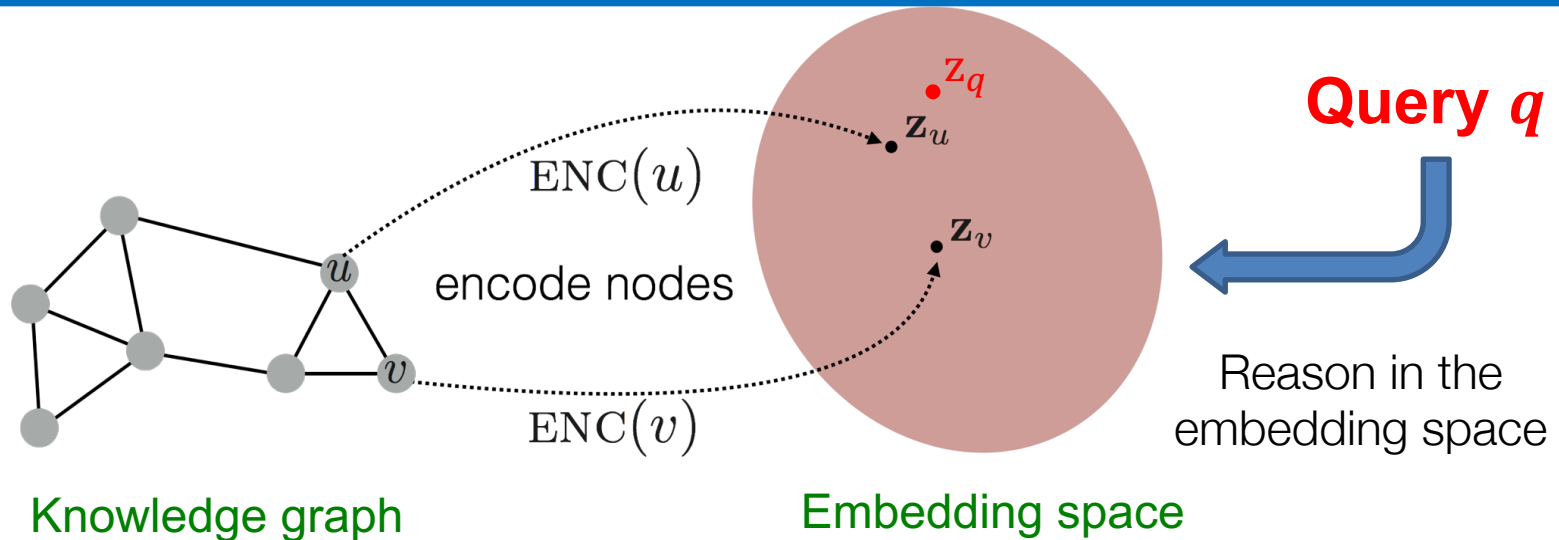
# Application (2): Fact Ranking

- Facts/Answers to queries are of **different importance/uncertainty** to users.

What's the **occupation** of **Selena Gomez**?



# Conclusion



- Box embeddings for answering logical queries on knowledge graphs
- Scalable query embeddings on massive KGs
- Applications towards neural query engine

# *Query2box: Reasoning over Knowledge Graphs in Vector Space Using Box Embeddings*

Hongyu Ren\*, Weihua Hu\*, Jure Leskovec  
ICLR 2020



# *Beta Embeddings for Multi-Hop Logical Reasoning in Knowledge Graphs*

Hongyu Ren, Jure Leskovec  
NeurIPS 2020



# *Latent Execution-Guided Reasoning for Multi-Hop Question Answering on Knowledge Graphs*

Hongyu Ren, Hanjun Dai, Bo Dai, Xinyun Chen, Michihiro Yasunaga, Haitian Sun, Dale Schuurmans, Jure Leskovec, Denny Zhou  
ICML 2021

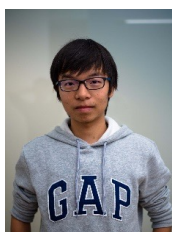


# *SMORE: Knowledge Graph Completion and Multi-hop Reasoning in Massive Knowledge Graphs*

Hongyu Ren\*, Hanjun Dai\*, Bo Dai, Xinyun Chen, Denny Zhou, Jure Leskovec, Dale Schuurmans  
KDD 2022



Weihua  
Hu



Hanjun  
Dai



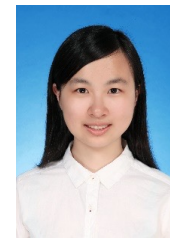
Bo  
Dai



Dale  
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Michihiro  
Yasunaga



Xinyun  
Chen



Denny  
Zhou



Jure  
Leskovec